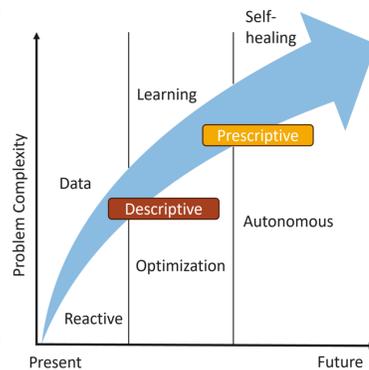


Physics-Informed Neural Networks for Distribution System State Estimation

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1. Motivation for Deep Learning in DSSE

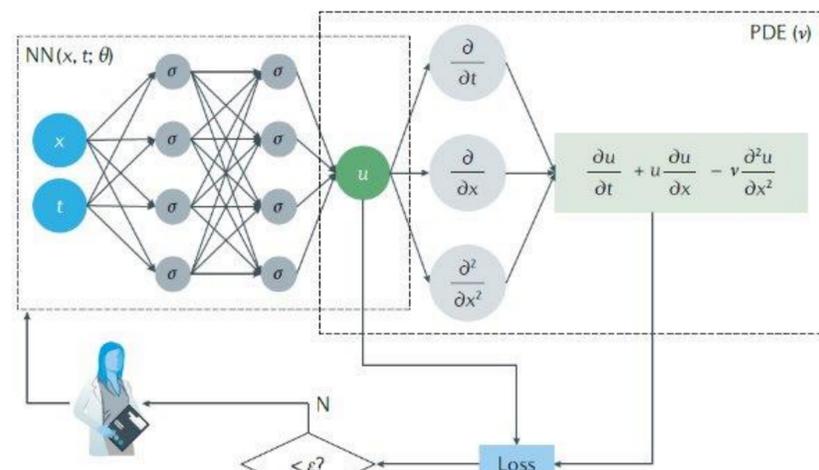
- Modern distribution networks growing due to aggressive DER integration.
- Challenges introduced to utilities conducting system health analysis due to various uncertainties – weather forecast models, load dynamics, topology shifts.
- WAM infrastructure, microPMUs, smart meters providing lots of data!
- Deep Learning (DL) emerging to solve complex problems in power systems, but...
 - Neural Networks often viewed as ‘black-box’ solutions, loss of interpretability.
 - Learning models may lack feasible solution space.
 - Must respect the underlying physical equations governing power system.



2. PINN Fundamentals

Algorithm 1: The PINN algorithm.

Construct a neural network (NN) $u(x, t; \theta)$ with θ the set of trainable weights w and biases b , and σ denotes a nonlinear activation function. Specify the measurement data $\{x_i, t_i, u_i\}$ for u and the residual points $\{x_j, t_j\}$ for the PDE. Specify the loss \mathcal{L} in Eq. (3) by summing the weighted losses of the data and PDE. Train the NN to find the best parameters θ^* by minimizing the loss \mathcal{L} .



$$\mathcal{L}_{data} = \frac{1}{N_{data}} \sum_{i=1}^N (u(x_i, t_i) - \hat{u}_i)^2$$

$$\mathcal{L}_{pde} = \frac{1}{N_{pde}} \sum_{j=1}^N \left(\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} - v \frac{\partial^2 u}{\partial x^2} \right)^2(x_j, t_j)$$

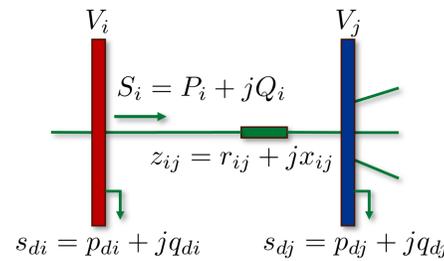
$$\mathcal{L}_{PINN} = w_{data} \mathcal{L}_{data} + w_{pde} \mathcal{L}_{pde} \quad (3)$$

Method & Drawbacks

- Surrogate model (DNN) and PDE residual for a PINN¹.
- Automatic differentiation on output for partial derivatives.
- Total loss function combines MSE metrics for both networks.
- Optimized via gradient descent on loss terms for parameter adjustments.
- Requires significant hyperparameter tuning and weight balancing to train.
- Additional constraints introduce more loss function terms: multi-objective.
- No feasible solution space guarantee.

3. Linearized Distribution Power Flow

- Traditional *Branch Flow Model*
- Neglect nonlinear terms for improved linear approximations
- Derive Linear Distribution Flow Model – **LEARN THIS!!**
- Can we train a PINN to approximate power flow while *learning the LinDistFlow model?*



Preliminaries:

$$P_{ij,t}^{pp} = \sum_{k:j \rightarrow k} P_{jk,t}^{pp} + P_{Load,j,t} - P_{DER,j,t} \quad \forall \rho \in \{a, b, c\} \quad (1)$$

$$Q_{ij,t}^{pp} = \sum_{k:j \rightarrow k} Q_{jk,t}^{pp} + Q_{Load,j,t} - Q_{DER,j,t} \quad \forall \rho \in \{a, b, c\} \quad (2)$$

$$3\phi = \rho_i, \phi_i \in \{a, b, c\} \quad v_{i,t}^\rho - v_{j,t}^\rho = \sum_{q \in \phi_{ij}} 2\Re[S_{ij,t}^{pq}(z_{ij}^{pq})^*] \quad \forall p, q \in \{a, b, c\} \quad (3)$$

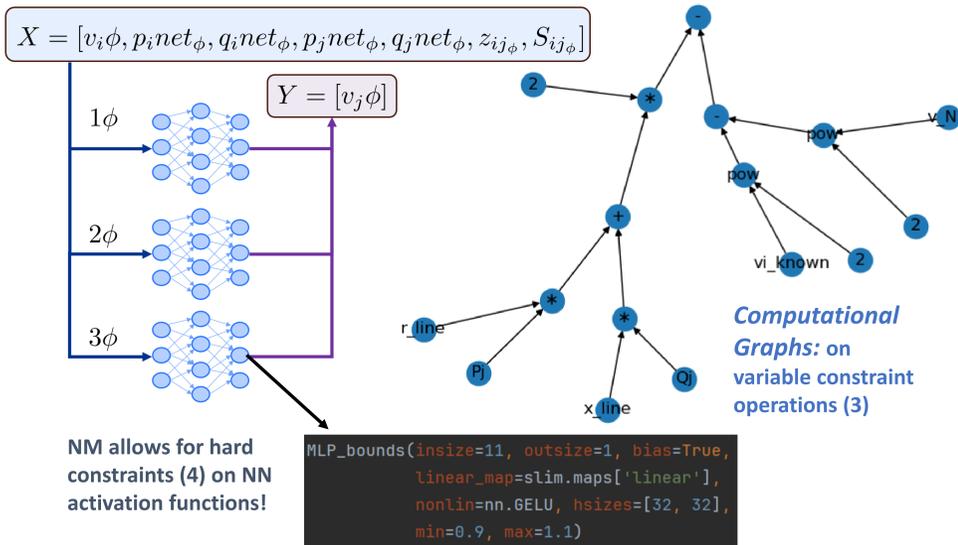
$$S_{ij}^{pq} = P_{ij}^{pq} + jQ_{ij}^{pq}, \quad pq \in \phi_{ij} \quad v_{min}^2 \leq v_{i,t}^\rho \leq v_{max}^2 \quad (4)$$

4. NeuroMANCER PINN Design & Simulation Study

- Open-source DP SciML library²
- Parametric constrained opt tasks
- PyTorch framework (wrapper)
- Build torch.NN structure
- Create Neuro-map from X:Y
- Define vars, obj, constraints
- Design problem, optimizer
- Train/Test Model



- IEEE 123bus system w/ 55 DERs
- Variable load dynamics
- QSTS, 5760 steps, 15 min step
- Conduct centralized load flow
- Select random lines, get bus pair info
- Collect LinDistFlow and DSS voltages
- Captures all physical state information in power system from measurements



NM allows for hard constraints (4) on NN activation functions!

Variables:

Symbolic Handlers

```
# vars from Dataset
x = variable('x')
r_line = x[:, 6]
x_line = x[:, 7]
Pj = x[:, 4]
Qj = x[:, 5]
```

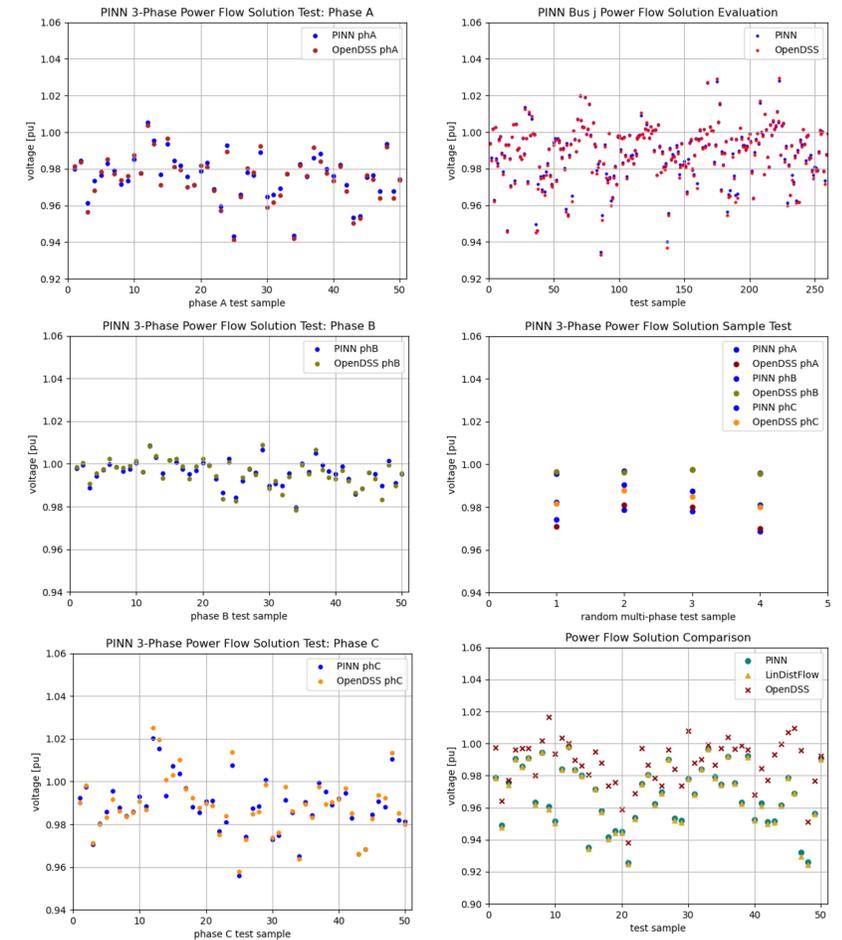
Objectives: inst variables or metric (torch.mean)

```
def get_objective():
    f_scale = 100 # speed up convergence
    mse_loss = f_scale * (v - v_target)**2
    obj = mse_loss.minimize(weight=1.0, name='obj')
    return obj
```

Constraints: variables (==, <, >, <=, >=) Returns dict {value, penalty, loss}

```
# power flow constraints
p_lhs = Pj
p_rhs = Pi - pj_net
p_con = (p_lhs == p_rhs)
p_con.name = 'pflow_con'
```

5. PINN Evaluation OpenDSS



Number Samples	5500
Batch	64
Mean Loss	0.0105
Train Penalty Loss	0.0111
Objective Loss	6.5021e-06
Constraint:	Violation: {a, b, c}
LDF Eq 1 Real PFlow	{0.0, 0.0, 0.0}
LDF Eq 2 Reactive PFlow	{0.0, 0.0, 0.0}
LDF Eq 3 Voltage Drop	{1.394e-03, 7.581e-04, 1.814e-03}
V bus2 limit >= 0.95 p.u.	{0.0, 0.0, 0.0}
V bus2 limit <= 1.05 p.u.	{0.0, 0.0, 0.0}

Number Samples	260
Batch	12
Mean Loss	0.0103
Test Penalty Loss	0.008
Objective Loss	3.2732e-06
Constraint:	Violation: {a, b, c}
LDF Eq 1 Real PFlow	{0.0, 0.0, 0.0}
LDF Eq 2 Reactive PFlow	{0.0, 0.0, 0.0}
LDF Eq 3 Voltage Drop	{4.404e-03, 2.469e-03, 7.367e-03}
V bus2 limit >= 0.95 p.u.	{0.0, 0.0, 0.0}
V bus2 limit <= 1.05 p.u.	{0.0, 0.0, 0.0}

6. Future Work Direction

- Train DSSE PINN on larger distribution feeders e.g. IEEE 8900 bus.
- Use the constrained PINN framework to solve more rigorous constrained optimization problems: DistOPF, etc.
- Use PINNs to determine unreported PV systems for the utility³.

7. References

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